

# Alternativní strategie pro SH tomografii

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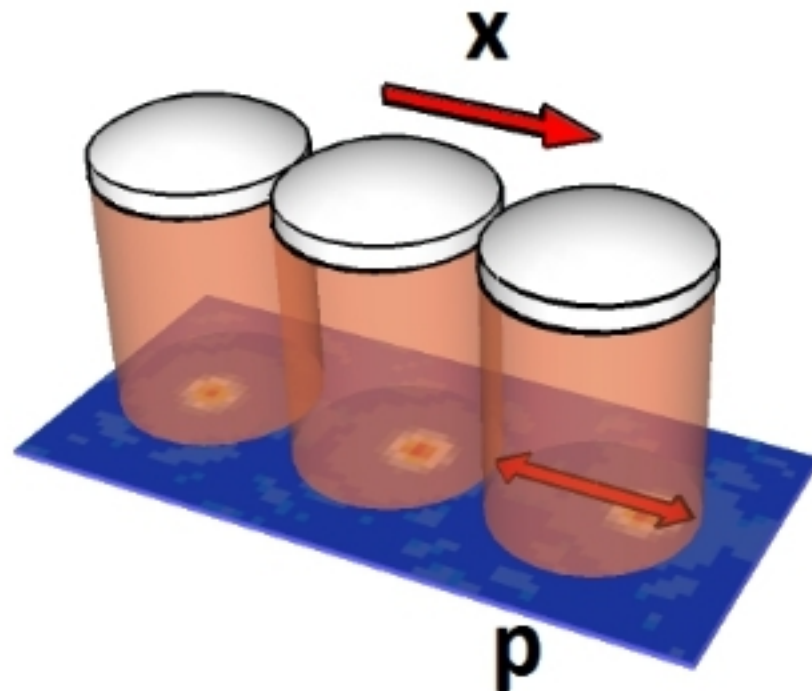
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# Shack-Hartmann detection

## *standard S-H detection*

- local wavefront tilts are measured
- wavefront is reconstructed
- what if there is no well-defined wavefront?



# SH-detection: detailed picture

## *system*

- external degrees of freedom of light
- described by coherence matrix  $\rho$
- notice that  $\rho \geq 0$

## *measurement*

- simultaneous position and momentum measurement

# Standard QSE

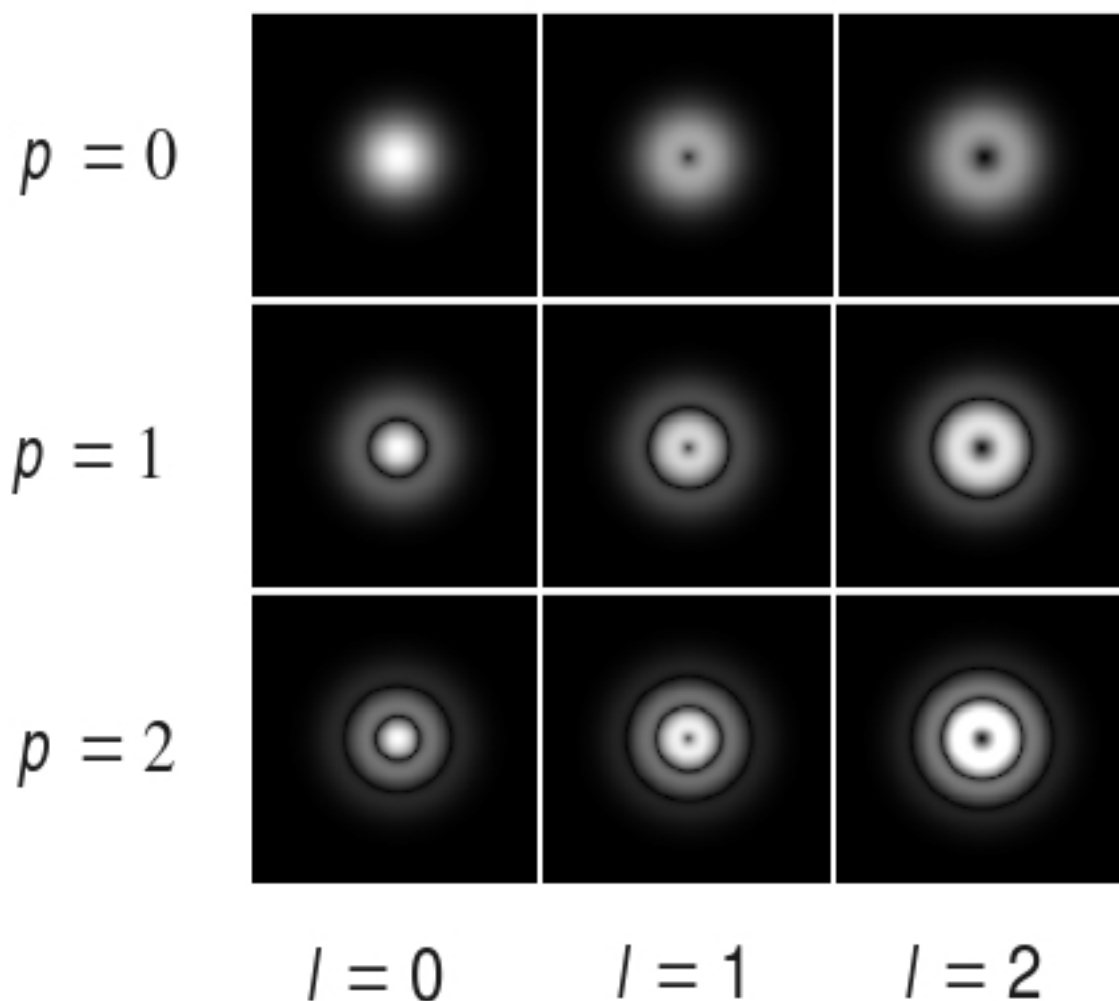
## *some known issues*

- knowledge of the measurement required
- result may strongly depend on the reconstruction space
- imperfect knowledge of the apparatus
  - bias
  - reconstruction artifacts
  - reconstruction breaks down

# Characterization of vortex beams

- Laguerre-Gaussian beams

$$LG_p^l(x, y) = \langle xy | lp \rangle \propto r^{|l|} L_p^{|l|}(2r^2) e^{-r^2} e^{il\varphi}$$

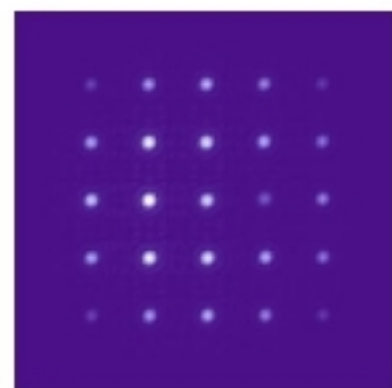


# Characterization ...

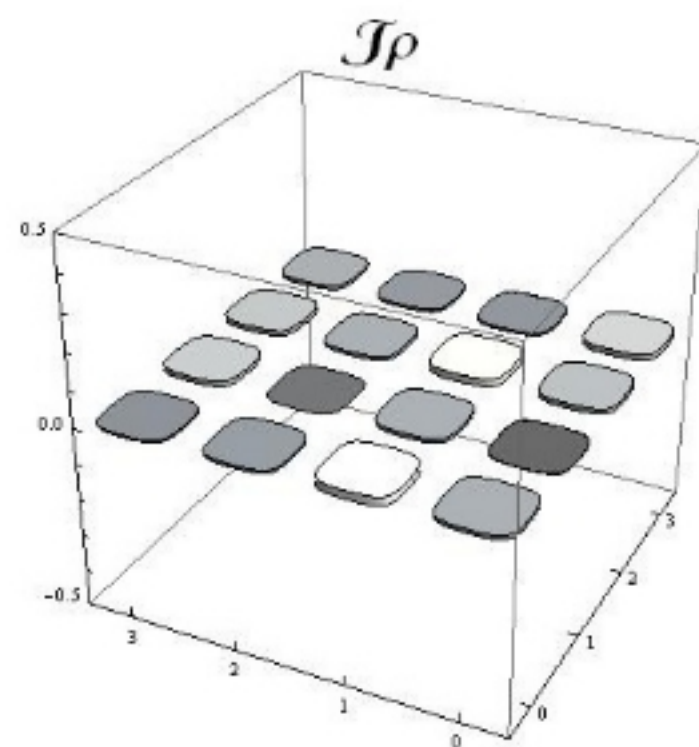
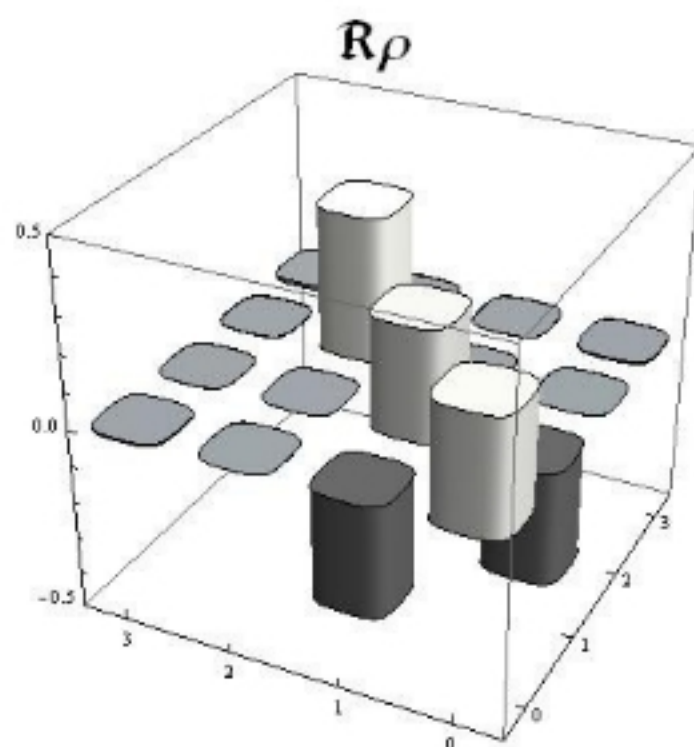
$$\rho_{\text{true}} = \frac{3}{5} |LG_0^0 - LG_0^1\rangle \langle LG_0^0 - LG_0^1| + \frac{2}{5} |LG_0^2\rangle \langle LG_0^2|$$



intensity

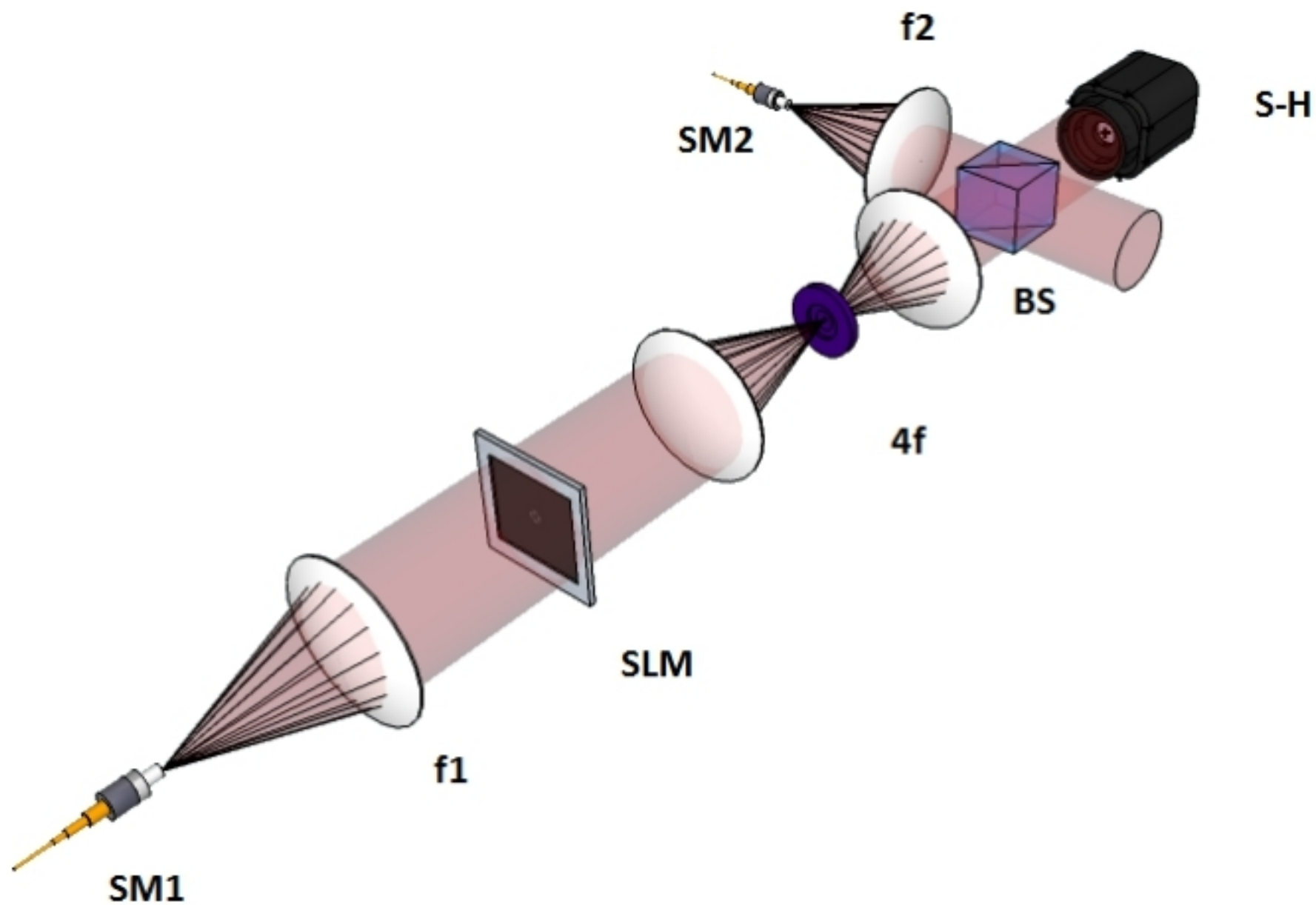


SH data



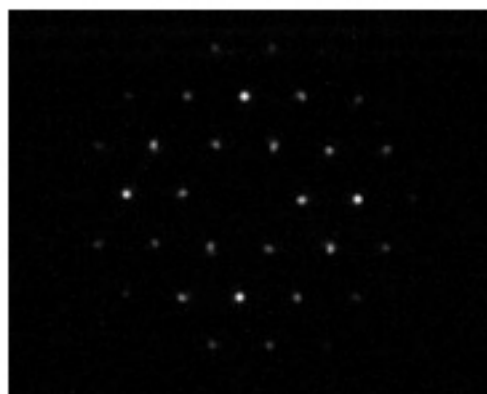
reconstruction from simulated data (5% noise)

# Experimental setup

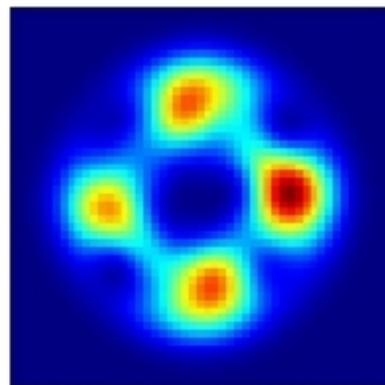


# Propagation of vortices

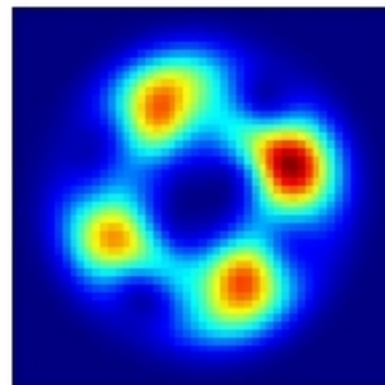
- target state  $|LG_0^4\rangle + |LG_0^8\rangle$



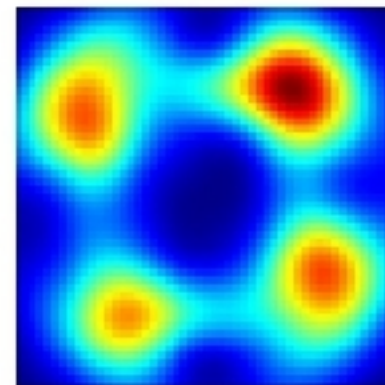
SH data



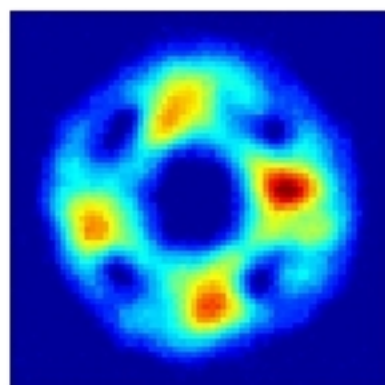
tomography



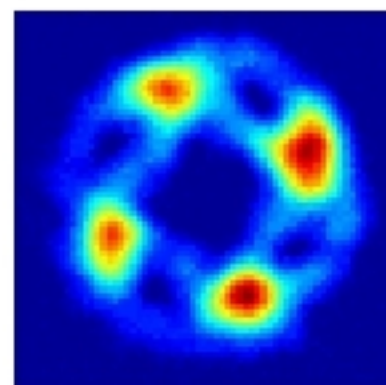
digital propagation



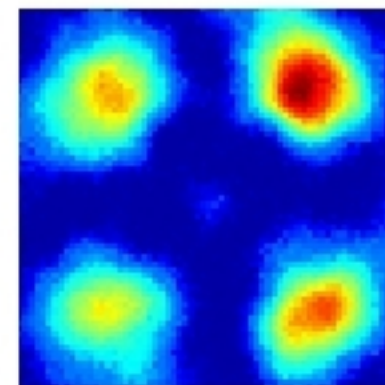
CCD



0 cm



17 cm



62 cm



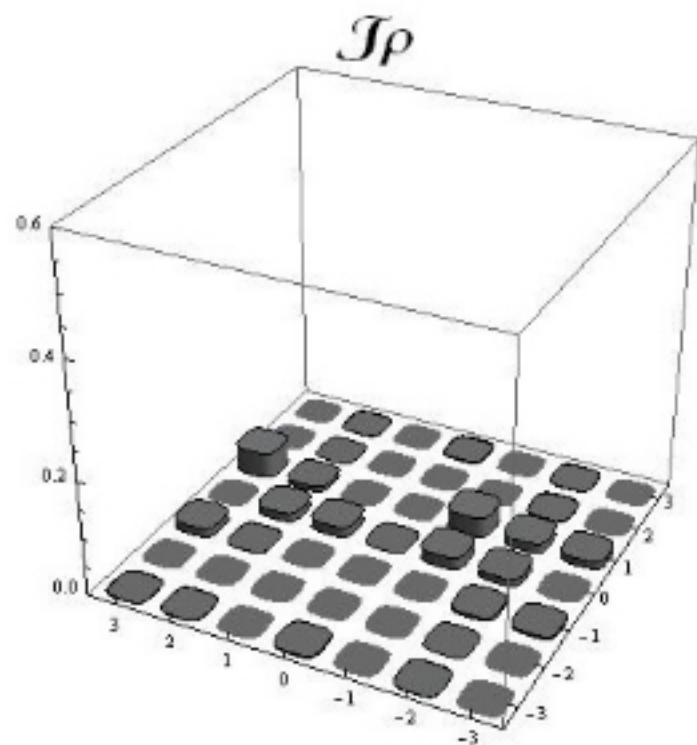
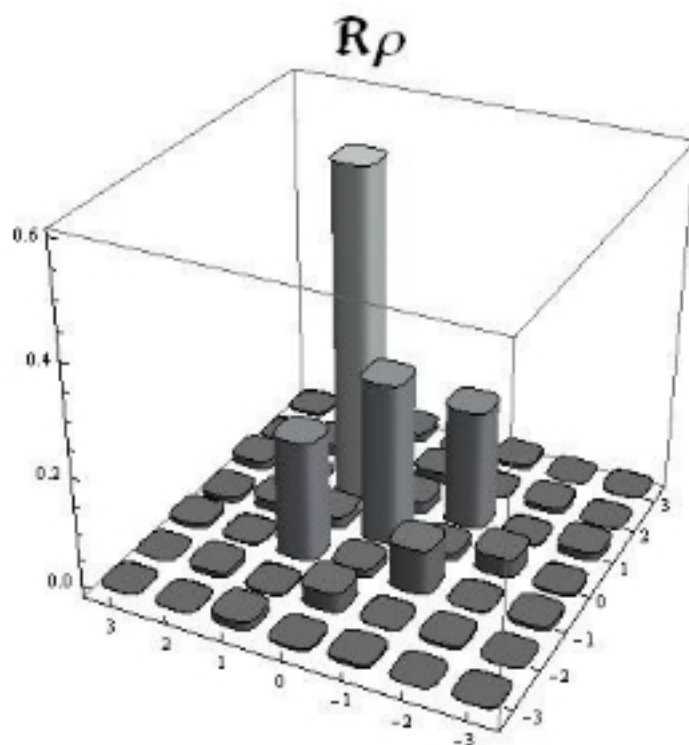
# Plane waves

- target state

$$\rho = |\Psi\rangle\langle\Psi| + \alpha |0\rangle\langle 0|, \quad |\Psi\rangle = |-1\rangle + \beta |1\rangle$$

angle w.r.t. optical axis

- reconstruction



# Data pattern tomography

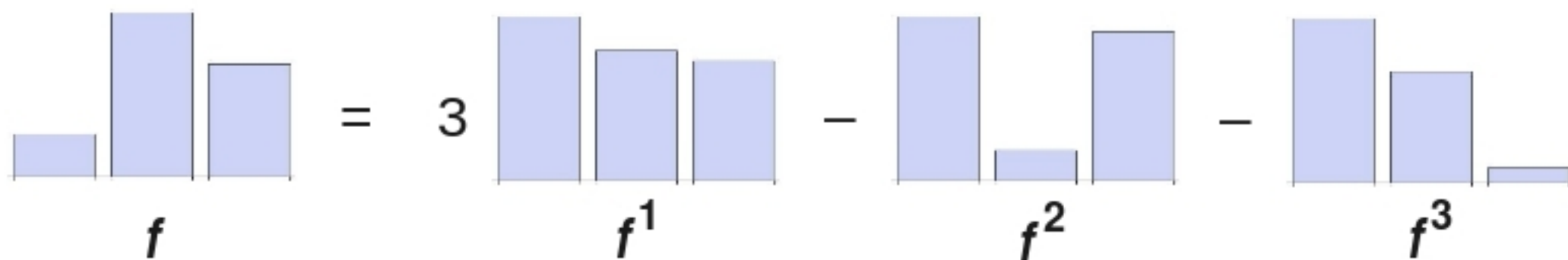
## *key features*

- prior knowledge of the apparatus is not required
- estimator is a mixture of experimentally feasible probe states
- reconstruction space is spanned by the probe states
- *field of view* is determined by the quantum resources used in the experiment

# Procedure

- probe states  $\sigma_k$  measured
- data patterns  $f_j^k$  recorded
- unknown state  $\rho$  measured and data  $f_j$  recorded
- best fit of  $f_j$  in terms of  $f_j^k$  found:  $f_{j,\text{est}} = \sum_k x_k f_j^k$
- estimator:  $\rho_{\text{est}} = \sum_k x_k \sigma_k$
- quantum theory enters the procedure through positivity constraints

# Very simple example



reconstruction:  $\rho = 3\sigma_1 - \sigma_2 - \sigma_3$

# Procedure

## *data pattern tomography*

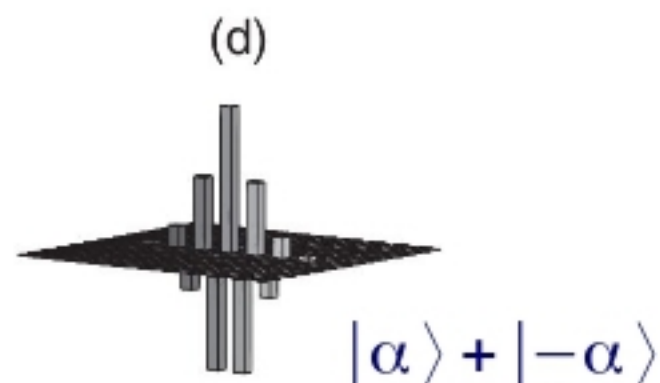
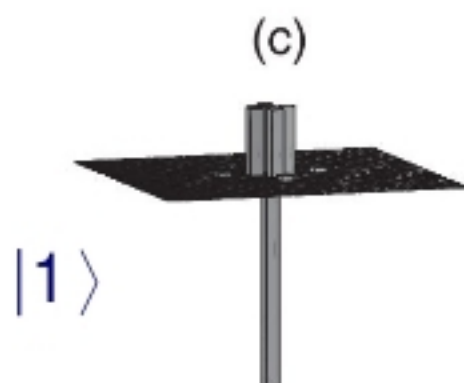
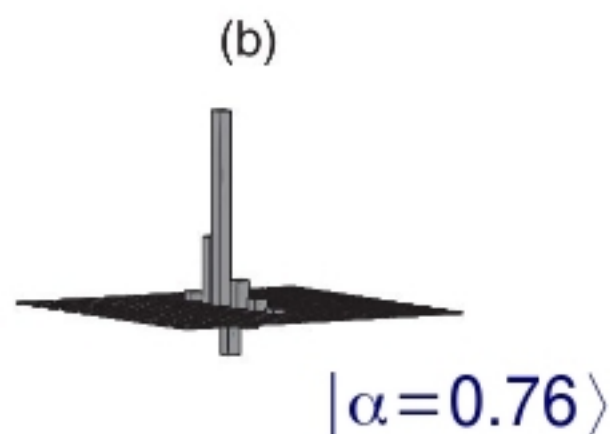
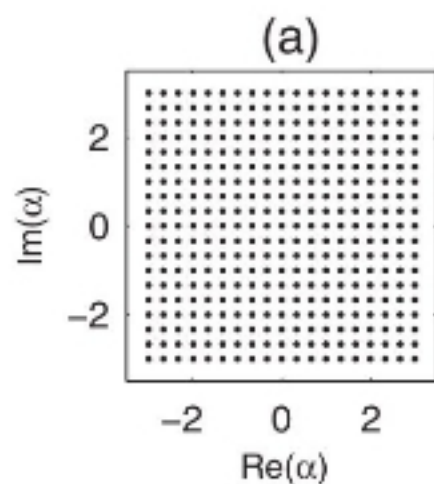
- find  $\mathbf{x}$  minimizing  $\text{dist}\left(\mathbf{f}, \sum_k x_k \mathbf{f}^k\right)$
- subject to  $\rho_{\text{est}} = \sum_k x_k \sigma_k$  being non-negative  $\rho_{\text{est}} \geq 0$

## *numerical implementation*

- primal-dual interior point method
  - barrier function
  - perturbed complementarity condition

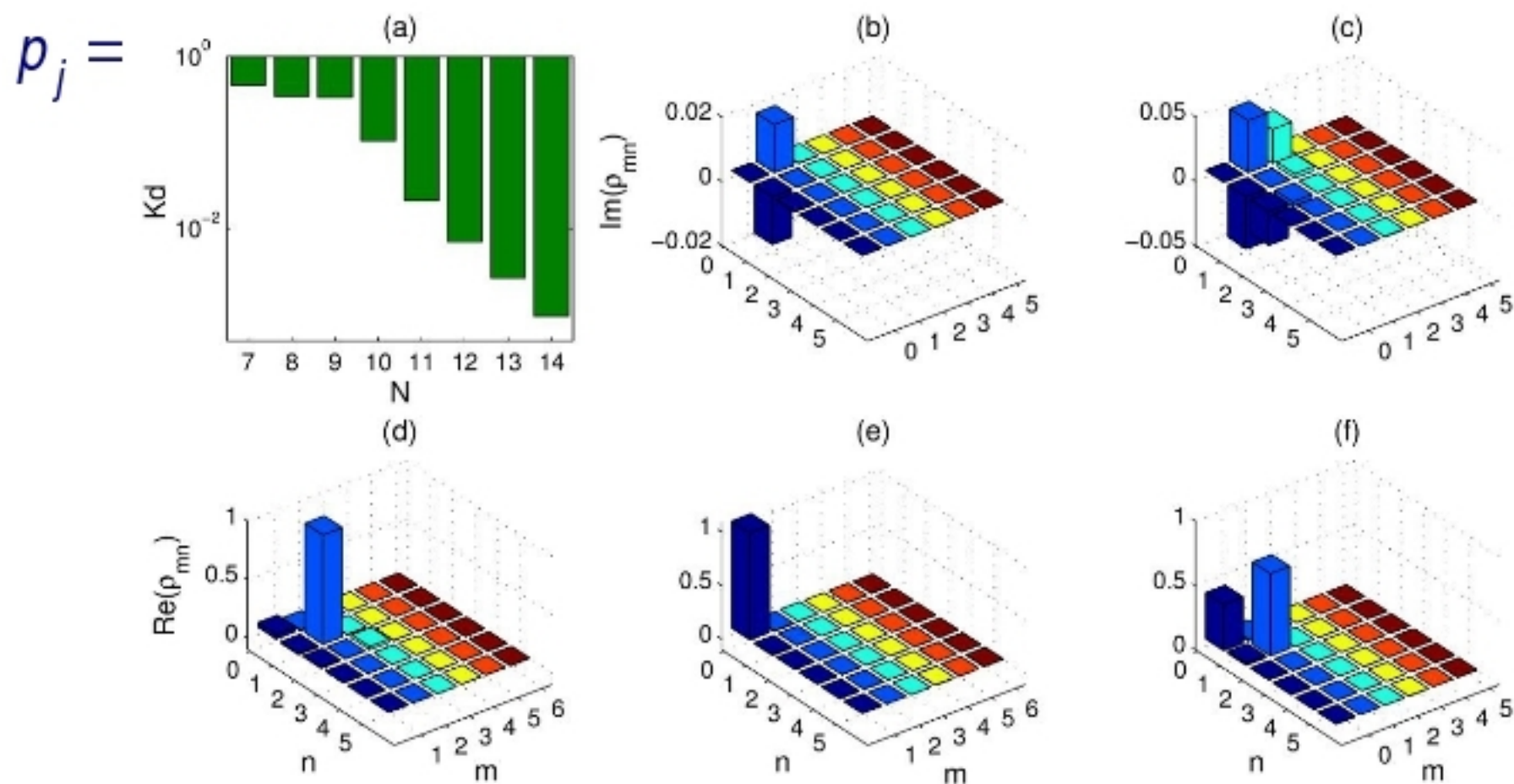
# State representation

- coherent-state representation



# Example: homodyne tomography

- phase-averaged coherent probe states



# Conclusions

- Data pattern tomography proposed for SH tomography.
- No prior calibration of the measurement apparatus is necessary.
- Tomography with unknown wavefront sensors is possible.
- *Field of view* is uniquely defined by the measurement.